





MPORTANT

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ORGANISATION AND **P**ROCEDURES

For full details, see the Members' Area

To ensure the integrity of the competition, the Olympiads must be administered under examination conditions.

DO

- Supervise students at all times
- Seat students apart
- Maintain silence
- Provide blank working paper
- Give time warnings when 3 minutes remain, and again when 1 minute remains
- Collect, mark and retain the papers

• Print the Olympiad papers prior to the Olympiad Date

DO NOT

- Read the questions aloud to the students
- Interpret the questions for students
- Permit any discussion or movement around the room
- Permit the use of calculators or other electronic devices
- Olympiad papers are scored by the PICO using the *Solutions and Answers* sheet provided.
- Results should be submitted in the Members' Area within 7 days of the Olympiad.
- Original student answer sheets should be retained by the PICO until the end of the year.
- *Solutions and Answers sheets* are not to be handed out to students. They are a teaching resource for use in class *after* completion of the Olympiad paper.

TIMING OF THE OLYMPIAD

- The *Total Time Allowed* for the Olympiad is **30 minutes**.
- The time for each individual question is a guide for the students.

ABSENT STUDENT POLICY

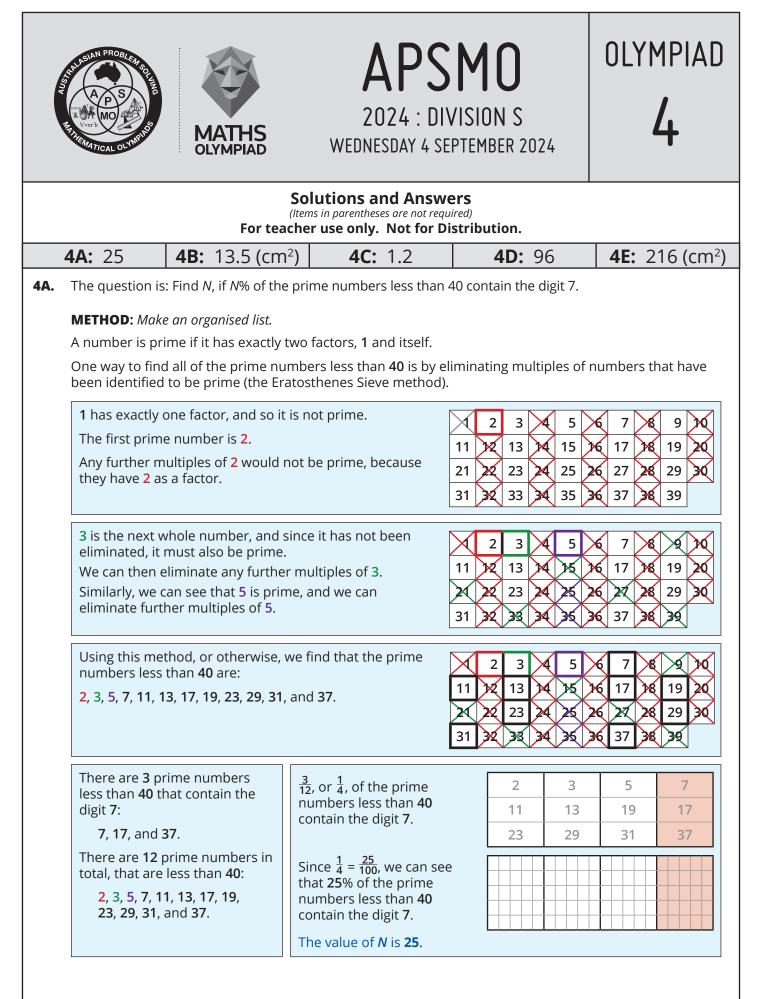
A student who is legitimately absent on the Olympiad date, may sit the Olympiad under examination conditions on their first day back at school (if that date is within 2 weeks of the original Olympiad date). If these conditions cannot be met, the student must be marked as absent on the submitted results.

The Absent Student Policy is available in the **Contest Administration** section of the Members' Area.

Acout Nr.	APSAUSE MATHS NUMERAL DIVISION S WEDNESDAY 4 SEPTEMBER 2024	olympiad 4					
Total Time Allowed: 30 Minutes Calculators NOT Permitted							
4A .	<i>N</i> % of the prime numbers less than 40 contain the digit 7. Find <i>N</i> .	Write your answers in the boxes on the back.					
4B.	In $\triangle PQR$, point S lies on side PR.The length of PS is 5 cm.The length of SR is 3 cm.The area of $\triangle PQR$ is 36 square cm.Find the area of $\triangle SQR$, in square cm.	Keep your answers hidden by folding backwards on this line.					
4C.	Express, as a decimal, the difference between $\sqrt{0.01}$ and $\frac{0.013}{0.01}$.						
4D.	A wooden cube is painted white and then cut into unit cubes. Each unit cube measures 1 cm × 1 cm × 1 cm. There are forty-eight unit cubes with exactly two faces painted white. How many of the unit cubes have exactly one face painted white?						
4E.	The given star pattern is composed of four identical right-angled triangles. The longest side of each right-angled triangle has length 15 cm. The other two sides differ in length by 3 cm, as shown. Find the total area of the star pattern, in square cm.						

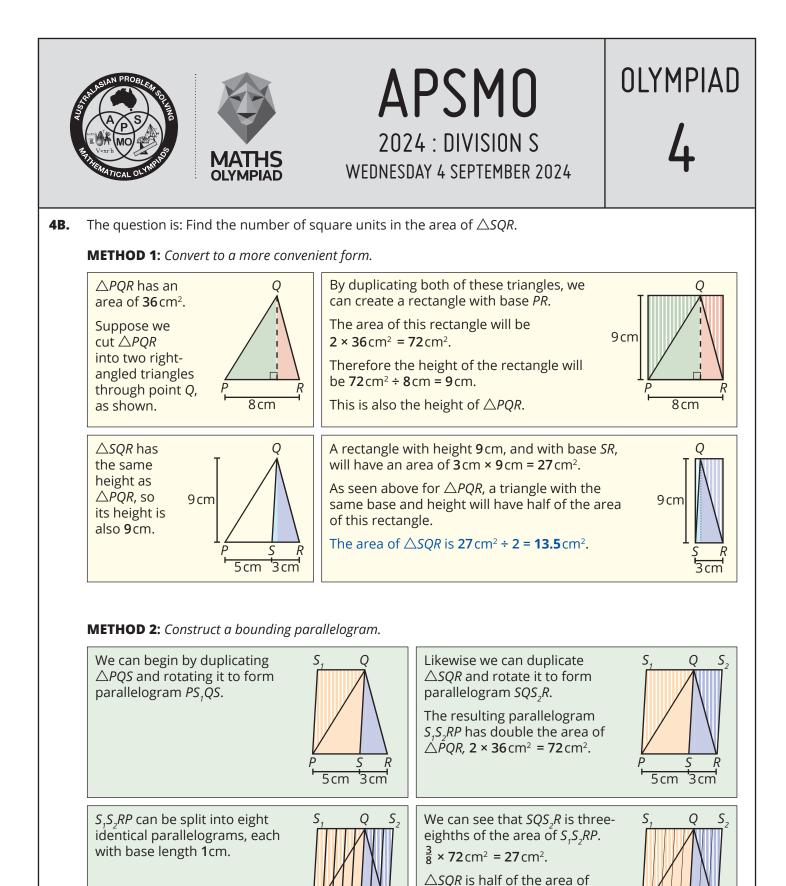
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A CONTINUES OF THE OFFICE OFFI	MATHS OLYMPIAD	APSMO 2024 : DIVISION S WEDNESDAY 4 SEPTEMBER 2024	olympiad 4
4A .	Student Name:		
4B.	Fold here. Keep your answers hidden.		
4C.	answers hidden.		
4D.			
4E.			



Follow-UP: K% of the prime numbers less than 100 contain the digit 2. Find K. [12]

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FOLLOW-UP: Point T lies on the line that passes through points P and R. If the area of \triangle PTQ is 45 cm², find all possible values for the length RT. [2 cm and 18 cm]

 $SQS_{2}R.$

The area of $\triangle SQR$ is **27** cm² ÷ **2** = **13.5** cm².

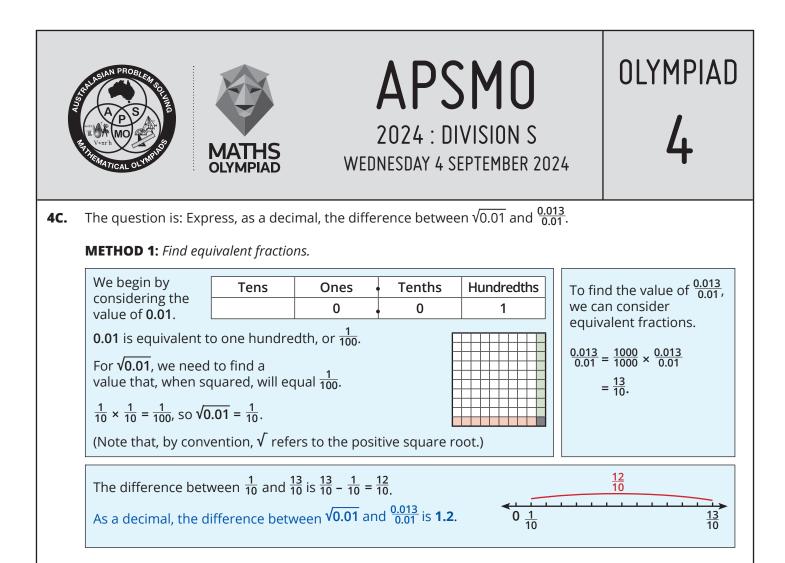
'? cm

5 cm

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<u>'3 cm</u>

5 cm



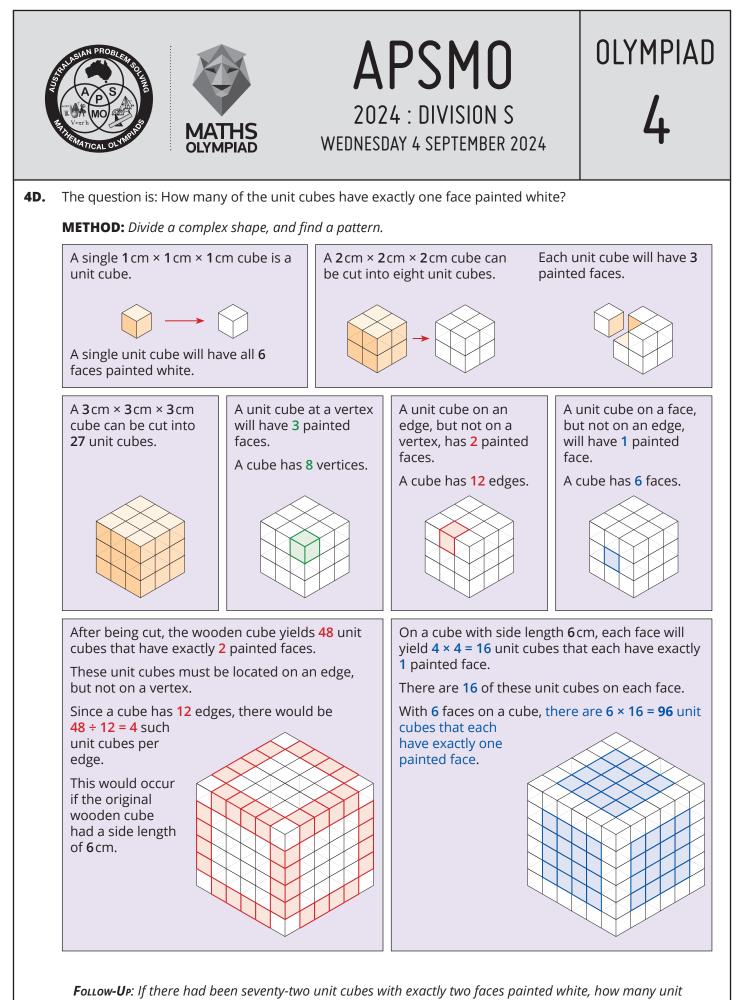
METHOD 2: Reason algebraically.

Let $\frac{a}{b} = \sqrt{0.01}$, where a and b are	e both positive.	Let $\frac{c}{d} = \frac{0.013}{0.01}$.	
Then:	$\frac{a}{b} \times \frac{a}{b} = 0.01$	Multiplying both sides by 0.01 :	$0.01\frac{c}{d} = 0.013$
	$\frac{a^2}{b^2} = 0.01$	Multiplying both sides by <i>d</i> :	0.01 <i>c</i> = 0.013 <i>d</i>
Multiplying both sides by b^2 :	$a^2 = 0.01b^2$	Multiplying both sides by 1000 :	10 <i>c</i> = 13 <i>d</i>
Multiplying both sides by 100 :	$100a^2 = b^2$	Dividing both sides by 10 :	<i>c</i> = 1.3 <i>d</i>
Square root both sides:	10 <i>a</i> = <i>b</i>	Dividing both sides by <i>d</i> :	$\frac{c}{d} = 1.3$
Dividing both sides by b :	$10 \times \frac{a}{b} = 1$	Therefore, <u>0.013</u> = 1.3.	
Dividing both sides by 10 :	$\frac{a}{b}=\frac{1}{10}.$		
Therefore, $\sqrt{0.01} = \frac{1}{10} = 0.1$.			

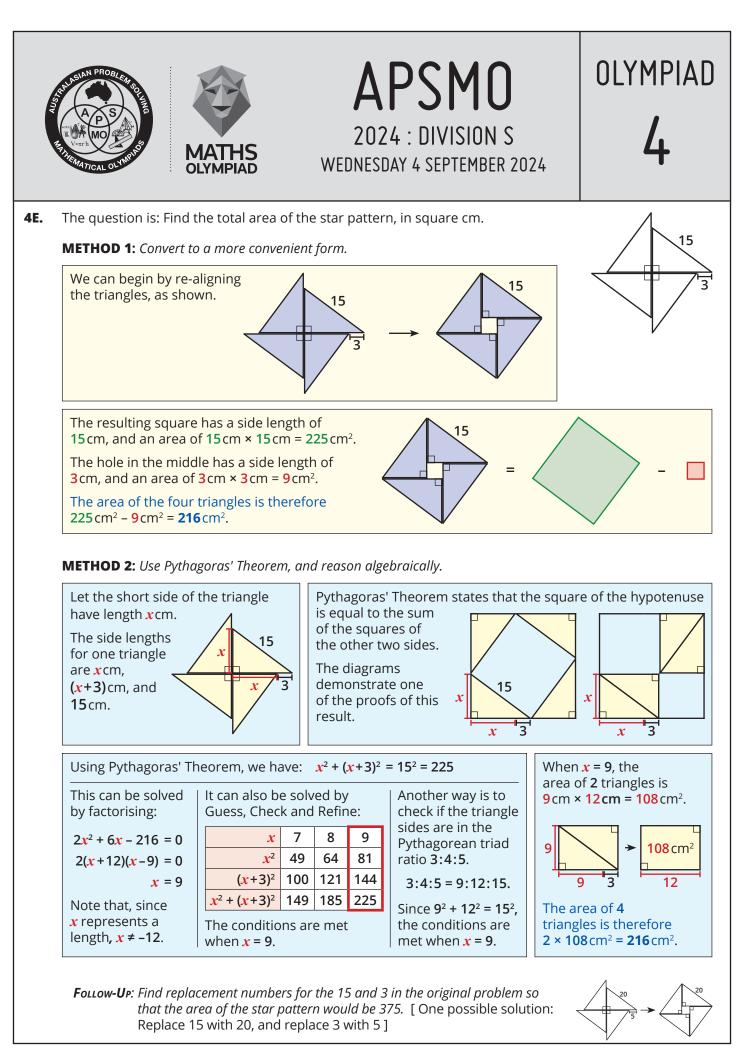
As a decimal, the difference between $\sqrt{0.01}$ and $\frac{0.013}{0.01}$ is 1.3 – 0.1 = 1.2.

FOLLOW-UP: Express, as a decimal, the difference between $\sqrt{0.0001}$ and $\frac{0.013}{0.0001}$. [129.99]

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cubes would have exactly one face painted white? [216]



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