



# APSMO

WEDNESDAY 3 MAY 2023

MATHS GAMES  
JUNIOR  
1

*Suggested Time: 30 Minutes*

**1A.** Hugo is using square tiles that are all the same size.

He begins with one white tile,



and then surrounds it with a border of 8 grey tiles.

1	2	3
8		4
7	6	5

He surrounds the grey tiles with a border of 16 white tiles.

1	2	3	4	5
16				6
15				7
14				8
13	12	11	10	9

Hugo continues to alternate between grey and white borders.

How many tiles will Hugo need for the next white border?

Hint: You could draw more tiles around Hugo's pattern.

**1B.** Buying two bottles of water and a bottle of juice from a vending machine costs \$10.

Two bottles of juice and one bottle of water costs \$11.

How much does it cost to buy one bottle of water from this vending machine, in dollars?

Hint: Is a bottle of water more or less expensive than a bottle of juice?

**1C.** Jeremy and Kaleb are building a fence around a paddock.

They start at one corner and work around in opposite directions to each other.

Jeremy takes 30 minutes to build one metre of fence.

Kaleb takes 10 minutes to build one metre of fence.

The perimeter of the paddock is 80 metres long.

How many more metres of fence will Kaleb build than Jeremy?

Hint: How much of the fence will Jeremy build in one hour?

**1D.** 15 divided by 6 is 2 remainder 3.

In total, how many different counting numbers will leave a remainder of 3 when divided into 15?

Hint: You could build a table.

**1E.** In the next 16 days, there will be 3 Fridays.

How many Tuesdays were there in the past 38 days?

Hint: What day of the week might it be today?

*Write your answers in the boxes on the back.*



*Keep your answers hidden by folding backwards on this line.*



**MATHS  
GAMES**

**APSMO**  
WEDNESDAY 3 MAY 2023

**MATHS GAMES  
JUNIOR  
1**

**1A.**

**Student Name:**

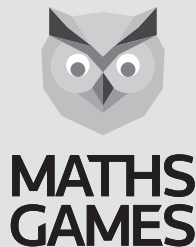
**1B.**

**1C.**

**1D.**

**1E.**

*Fold here. Keep your answers hidden.*



# APSMO

WEDNESDAY 3 MAY 2023

## MATHS GAMES JUNIOR 1

### Solutions and Answers

(Items in parentheses are not required)

1A: 32

1B: (\$)3

1C: 40

1D: 3

1E: 6

1A. The question is, How many tiles will Hugo need for the next white border?

#### Strategy 1: Build a Table, and Draw a Diagram

Let's use a table to record the number of tiles for each border.

Tile pattern				
Tiles in outside border	8	16	24	32

Hugo will need **32** tiles for the next white border.

#### Strategy 2: Build a Table, Draw a Diagram, and Find a Pattern

It may help to consider the side length for each pattern of squares.

Tile pattern				
Side length of pattern	3	5	7	9

Every time Hugo adds another border, the side length increases by 2.

We can then use many different methods to count the tiles in the outside border. For example, for a side length of 5:

$5 + 3 + 5 + 3 = 16$	$4 \times 3 + 4 = 16$	$4 \times 4 = 16$	$(5 \times 5) - (3 \times 3) = 16$

These patterns can then be applied to larger side lengths.

We want to find the number of tiles in the outside border, for a side length of 9.

$9 + 7 + 9 + 7 = 32$	$4 \times 7 + 4 = 32$	$4 \times 8 = 32$	$(9 \times 9) - (7 \times 7) = 32$

Regardless of the method we choose to use, we find that Hugo needs **32** tiles for the next white border.

**Follow-Up:** How many tiles would there be in the white border after this one? [ 48 ]



# APSMO

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## MATHS GAMES JUNIOR 1

**1B.** The question is, How much does it cost to buy one bottle of water, in dollars?

**Strategy 1: Build a Table, and Find a Pattern**

Let's guess that a bottle of water costs \$1.

Since 2 bottles of water and 1 bottle of juice costs \$10,  
1 bottle of juice must cost  $\$10 - 2 \times \$1 = \$8$ .

If so, 2 bottles of juice and 1 bottle of water would cost  $2 \times \$8 + \$1 = \$17$ .

1 Water	1 Juice	2 Juice + 1 Water
\$1	\$8	$2 \times \$8 + \$1 = \$17$

If a bottle of water costs \$2, 1 bottle of juice must cost  
 $\$10 - 2 \times \$2 = \$6$ .

2 bottles of juice and 1 bottle of water would cost  
 $2 \times \$6 + \$2 = \$14$ .

1 Water	1 Juice	2 Juice + 1 Water
\$1	\$8	$2 \times \$8 + \$1 = \$17$
\$2	\$6	$2 \times \$6 + \$2 = \$14$

Increasing the cost of the water by \$1 reduced the total cost for 2 bottles of juice + 1 bottle of water by \$3.  
We want to reduce the total cost for 2 bottles of juice + 1 bottle of water down by another \$3, to \$11.  
Let's try increasing the cost of the water by another \$1.

If a bottle of water costs \$3, 1 bottle of juice must cost  
 $\$10 - 2 \times \$3 = \$4$ .

2 bottles of juice and 1 bottle of water would cost  
 $2 \times \$4 + \$3 = \$11$ .

That matches the question.

1 Water	1 Juice	2 Juice + 1 Water
\$1	\$8	$2 \times \$8 + \$1 = \$17$
\$2	\$6	$2 \times \$6 + \$2 = \$14$
\$3	\$4	$2 \times \$4 + \$3 = \$11$

One bottle of water costs \$3.

**Strategy 2: Draw a Diagram and Reason Logically**

1 bottle of juice and  
2 bottles of water  
costs \$10.



2 bottles of juice and  
1 bottle of water costs  
\$11.



All together, 3 bottles of juice and 3 bottles of  
water would cost  $\$10 + \$11 = \$21$ .



We can arrange 3 bottles of juice and 3 bottles  
of water into 3 equal groups, each containing  
1 juice and 1 water.



If the 3 groups cost \$21 all together, one of  
the groups, with 1 juice and 1 water, must cost  
 $\$21 \div 3 = \$7$ .

1 bottle of juice and  
2 bottles of water  
costs \$10.

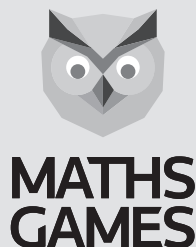


1 bottle of juice and  
1 bottle of water  
costs \$7.



Therefore, one bottle of water by itself must cost  
 $\$10 - \$7 = \$3$ .

**Follow-Up:** If it costs \$24 for 2 bottles each of water, juice and soft drink, how much does 1 bottle of soft drink cost? [ \$5 ]



# APSMO

WEDNESDAY 3 MAY 2023

## MATHS GAMES JUNIOR 1

1C. The question is, how many more metres of fence would Kaleb build than Jeremy?

### Strategy 1: Build a Table, and Find a Pattern (1)

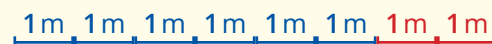
Kaleb builds 1 metre of fence every 10 minutes.  
Since there are  $6 \times 10 = 60$  minutes in an hour, in one hour Kaleb would build **6 metres** of fence.

Fence Length		
Time	10 mins	$6 \times 10 = 60$ mins (= 1 hour)

Jeremy builds 1 metre of fence every 30 minutes.  
Since there are  $2 \times 30 = 60$  minutes in an hour, in one hour Jeremy would build **2 metres** of fence.

Fence Length		
Time	30 mins	$2 \times 30 = 60$ mins (= 1 hour)

Working together, in one hour Kaleb and Jeremy will build **6 metres** + **2 metres** = **8 metres** of fence.



If Kaleb and Jeremy build 8 metres of fence in an hour, then in 10 hours they will build  $10 \times 8 = 80$  metres of fence.

80 metres is the amount required to go around the paddock.

In 10 hours, **Kaleb builds 60 metres of fence**, and **Jeremy builds 20 metres of fence**.

So **Kaleb would build  $60 - 20 = 40$  more metres of fence than Jeremy**.

Time (hours)	1	2	3	...	10
Kaleb's Fence (m)	6	12	18	...	60
Jeremy's Fence (m)	2	4	6	...	20
Total Fence (m)	8	16	24	...	80

### Strategy 2: Build a Table, and Find a Pattern (2)

Jeremy builds **1 metre of fence** in 30 minutes.

Kaleb builds **1 metre of fence** in 10 minutes, so in  $3 \times 10 = 30$  minutes he will build  **$3 \times 1 = 3$  metres of fence**.

When Kaleb and Jeremy build  $3 + 1 = 4$  metres of fence together, Kaleb ends up building  $3 - 1 = 2$  metres more than Jeremy.

The difference is **half** of the total amount of fence built so far.

Jeremy's Fence (m)	1				
Kaleb's Fence (m)	3				
Total Fence (m)	4				
Difference (m)	2				

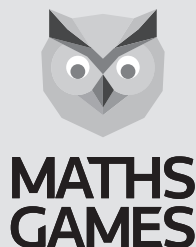
If we continue the table, we can see that the difference continues to be **half** of the total amount of fence built so far.

Why does this pattern occur?

Jeremy's Fence (m)	1	2	3	...	
Kaleb's Fence (m)	3	6	9	...	
Total Fence (m)	4	8	12	...	80
Difference (m)	2	4	6	...	40

When the 80m fence is complete, **Kaleb will have built  $80 \div 2 = 40$  metres more than Jeremy**.

**Follow-Up:** Jeremy and Kaleb agree to build half of the 120m fence each. After he has finished his half, for how many hours does Kaleb need to wait until Jeremy has finished his half? [ 20 ]



# APSMO

WEDNESDAY 3 MAY 2023

## MATHS GAMES JUNIOR 1

**1D.** The question is, How many different counting numbers will leave a remainder of 3 when divided into 15?

### Strategy 1: Build a Table

We can try dividing 15 by every counting number that is less than, or equal to, 15.

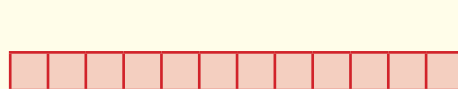
Divisor	Division and Remainder	Divisor	Division and Remainder	Divisor	Division and Remainder
1	$15 \div 1 = 15$ r. 0	6	$15 \div 6 = 2$ r. 3	11	$15 \div 11 = 1$ r. 4
2	$15 \div 2 = 7$ r. 1	7	$15 \div 7 = 2$ r. 1	12	$15 \div 12 = 1$ r. 3
3	$15 \div 3 = 5$ r. 0	8	$15 \div 8 = 1$ r. 7	13	$15 \div 13 = 1$ r. 2
4	$15 \div 4 = 3$ r. 3	9	$15 \div 9 = 1$ r. 6	14	$15 \div 14 = 1$ r. 1
5	$15 \div 5 = 3$ r. 0	10	$15 \div 10 = 1$ r. 5	15	$15 \div 15 = 1$ r. 0

There are **3** different counting numbers that leave a remainder of 3 when divided into 15.

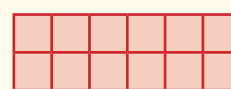
### Strategy 2: Draw a Diagram

If a number leaves a remainder of 3 when divided into 15, then it must be a factor of  $15 - 3 = 12$ .

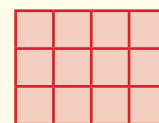
The factors of 12 are:



1 and 12,



2 and 6,



3 and 4.

Let's try dividing 15 by all of the factors of 12.

The remainder from a division must be less than the divisor. This means that, when we divide 15 by a number that is less than or equal to 3, any remainder must be less than 3.

$15 \div 1 = 15$  r. 0    
  $15 \div 2 = 7$  r. 1    
  $15 \div 3 = 5$  r. 0

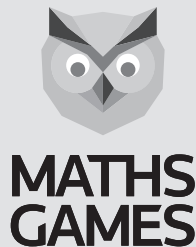
If we divide 15 by a factor of 12 that is greater than 3, the remainder will be exactly 3.

$15 \div 4 = 3$  r. 3    
  $15 \div 6 = 2$  r. 3

$15 \div 12 = 1$  r. 3

There are **3** different counting numbers that leave a remainder of 3 when divided into 15.

**Follow-Up:** How many numbers will leave a remainder of 3 when divided into 27? [ 5 (4, 6, 8, 12, 24) ]



# APSMO

WEDNESDAY 3 MAY 2023

## MATHS GAMES JUNIOR 1

1E. The question is, How many Tuesdays were there in the past 38 days?

"In the next 16 days" means 16 days starting from tomorrow.

"In the past 38 days" means 38 days, where the last of the 38 days was yesterday.



**Strategy: Build a Table, and Find a Pattern**

There will be 3 Fridays in the next 16 days.

Let's draw a calendar, to find out how many days we need, to be able to fit in 3 Fridays.

To get 3 Fridays, we will need at least 15 days.

Sun	Mon	Tue	Wed	Thu	Fri	Sat
					1	2
3	4	5	6	7	8	9
10	11	12	13	14	15	

The **extra (16th) day** of the "next 16 days" could either be just before, or just after these 15 days.

If so, today must be either Wednesday or Thursday.

Sun	Mon	Tue	Wed	Thu	Fri	Sat
			Today	16		

Sun	Mon	Tue	Wed	Thu	Fri	Sat
				Today		
						16

We can now figure out how many Tuesdays there were in the past 38 days.

Suppose today is a Wednesday. Let's count back.

We need to go back 1 day to get to the previous Tuesday.

Going back  $1 + 7 = 8$  days gets 2 previous Tuesdays, and so on.

Sun	Mon	Tue	Wed	Thu	Fri	Sat
38	37	36				
		29				
		22				
		15				
		8				
		1	Today	16		

What if today is a Thursday?

We need to go back 2 days to get to the previous Tuesday.

Going back  $2 + 7 = 9$  days gets 2 previous Tuesdays, and so on.

Sun	Mon	Tue	Wed	Thu	Fri	Sat
	38	37				
		30				
		23				
		16				
		9				
		2		Today		
						16

In both cases, we can see that there were 6 Tuesdays within the past 38 days.

**Follow-Up:** How many Thursdays were there in the past 38 days? [ 5 ]